



ANSWER BOOK

Moments and equilibrium

Mechanics · Year 12

AQA 3.4.1.2 · CIE 4.1.1, 4.1.2, 4.1.3, 4.1.4, 4.2.1, 4.2.2
OCR A 3.2.3(a), 3.2.3(b), 3.2.3(c), 3.2.3(d), 3.2.3(e)

19 questions · 58 marks

NAVY EDITION

SECTION A · Warm-up

- A1** Moment = force $\times$ perpendicular distance from the pivot to the line of action of the force (1). Unit: newton metre, N m (1). [2]
- A2** Moment = 15×0.40 (1) [2]
Moment = 6.0 N m (1)
- A3** For a body in equilibrium, the sum of the clockwise moments about any point (1) equals the sum of the anticlockwise moments about that point (1). [2]

SECTION B · Standard

- B1** Clockwise moment = anticlockwise moment: $2.0 \times 0.20 = 4.0 \times d$ (1) [3]
 $d = (2.0 \times 0.20)/4.0$ (1)
 $d = 0.10$ m to the right of the pivot (1)
- B2** Clockwise moment = anticlockwise moment: $300 \times 1.2 = 450 \times d$ (1) [3]
 $d = (300 \times 1.2)/450$ (1)
 $d = 0.80$ m (1)
- B3** Taking moments about A: $R_B \times 4.0 = 120 \times 2.0 + 200 \times 1.0$ (1) [4]
 $R_B = 110$ N (1)
Vertically: $R_A = (120 + 200) - 110$ (1)
 $R_A = 210$ N (1)
- B4** This is a couple (1) [3]
Its moment (torque) = one force $\times$ the separation = 8.0×0.25 (1)
Moment = 2.0 N m (1)

SECTION C · Stretch

- C1** Moments about the hinge: $T \times 2.0 = 40 \times 1.0$ (1) [4]
 $T = 20$ N (1)
Vertically: hinge force = $40 - 20$ (1)
Hinge force = 20 N upwards (1)

C2 The centre of mass is $(0.65 - 0.40) = 0.25$ m from the pivot (1) [4]
 Moments about the pivot: $2.0 \times 0.40 = W \times 0.25$ (1)
 $W = 0.80 / 0.25$ (1)
 $W = 3.2$ N (1)

C3 The moment of the applied force equals force $\times$ perpendicular distance from the hinge (1). Placing the handle far from the hinge maximises that distance (1), so a smaller force produces the moment needed to open the door (1). [3]

SECTION A · Warm-up

A4 Moment = 300×0.17 (1) = 51 N m (1). [2]

A5 The resultant force on the body is zero (1). The resultant moment about any point is zero (1). [2]

A6 The perpendicular distance from the pivot to the line of action is zero, so the moment $F \times d$ is zero (1). [1]

SECTION B · Standard

B5 Perpendicular distance = $0.240 \sin 55^\circ$ (240 mm converted to m) (1). Moment = $90 \times 0.240 \times \sin 55^\circ$ (1) = 17.7 N m (1). [3]

B6 The rule is uniform, so its weight 1.18 N acts at the 50.0 cm mark, 0.150 m from the pivot (1). Moments about the pivot: $W \times 0.300 = 1.18 \times 0.150$ (1), so $W = 0.59$ N (1). Mass = $W/g = 60$ g (0.060 kg) (1). [4]

B7 Moments about the pivot: $F \times 0.045 = 120 \times 0.55$ (1), so $F = 66/0.045$ (1) = 1467 N ≈ 1.5 kN (1). [3]

SECTION C · Stretch

C4 Taking moments about A with the decorator a distance x from A: $R_B \times 3.0 = 150 \times 1.5 + 720x$ (1). With $x = 3.0$ m, $R_B = 795$ N, which exceeds 600 N, so the decorator cannot reach B (1). Setting $R_B = 600$ N: $600 \times 3.0 = 225 + 720x$ (1), so $x = 2.2$ m from A (1). [4]

C5 The component of the tension perpendicular to the bar is $T \sin 30^\circ$, acting 1.2 m from the hinge (1). Moments about the hinge: $T \sin 30^\circ \times 1.2 = 35 \times 0.60 + 90 \times 1.0$ (1), so $0.60T = 111$ N m (1), giving $T = 185$ N (1). [4]

- C6** Place the rule on the pivot away from its centre and position the 50 g mass on the shorter side, adjusting until the rule balances horizontally (1). Measure the distance d_1 from the pivot to the centre of the 50 g mass, and the distance d_2 from the pivot to the 50.0 cm mark (1). The weight of a uniform rule acts at its centre of mass, the 50.0 cm mark (1). By the principle of moments: $0.050g \times d_1 = mg \times d_2$, so $m = 0.050 d_1/d_2$ (g cancels) (1). Repeat with the pivot at different positions and average the values of m to reduce random error (1). [5]
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