



ANSWER BOOK

Refraction and total internal reflection

Waves · Year 12

AQA 3.3.2.3 · OCR A 4.4.1(f)(i), 4.4.2(d)(i), 4.4.2(e)

18 questions · 52 marks

NAVY EDITION

SECTION A · Warm-up

- A1** Refractive index n = speed of light in a vacuum / speed of light in the material [2]
 $= c/v$ (1). It is always greater than or equal to 1 (1).
- A2** $n = c/v = (3.0 \times 10^8)/(2.0 \times 10^8)$ (1) [2]
 $n = 1.5$ (1)
- A3** The light must be travelling in the more optically dense medium (higher n) [2]
 towards the boundary with a less dense one (1), and the angle of incidence must exceed the critical angle (1).
- A4** The speed decreases and the wavelength decreases in the same ratio (1). The [2]
 frequency is unchanged (1).
- A5** Total internal reflection requires the light to be travelling towards a medium of [2]
 lower refractive index (1). Air has a lower refractive index than glass, so this light is
 heading into the denser medium and no critical angle exists: $\sin \theta_c = n_2/n_1$ would be
 greater than 1 (1).

SECTION B · Standard

- B1** $n_1 \sin \theta_1 = n_2 \sin \theta_2$ (1) [3]
 $\sin \theta_2 = \sin 40^\circ / 1.5$ (1)
 $\theta_2 = 25.4^\circ$ (1)
- B2** $\sin \theta_c = 1/n = 1/1.5$ (1) [2]
 $\theta_c = 41.8^\circ$ (1)
- B3** $\lambda_{\text{glass}} = \lambda/n = 600/1.5$ (1) [3]
 $= 400 \text{ nm}$ (1)
 $v = c/n = (3.0 \times 10^8)/1.5 = 2.0 \times 10^8 \text{ m s}^{-1}$ (1)
- B4** $n_1 \sin \theta_1 = n_2 \sin \theta_2$ (1) [3]
 $1.33 \times \sin 30^\circ = 1 \times \sin \theta_2$ (1)
 $\theta_2 = 41.7^\circ$ (1)
- B5** The angle of incidence is measured from the normal: $\theta_1 = 90^\circ - 25^\circ = 65^\circ$ (1). [3]
 $\sin \theta_2 = \sin 65^\circ / 1.33$ (1), so $\theta_2 = 43.0^\circ$ (1).

B6 $n_1 \sin \theta_1 = n_2 \sin \theta_2$: $\sin \theta_2 = 1.52 \times \sin 50^\circ / 1.66$ (1), so $\theta_2 = 44.5^\circ$ (1). The ray bends towards the normal because it enters the optically denser medium, where light travels more slowly (1). [3]

B7 Rays reflecting along the fibre at different angles travel different total distances, so parts of a pulse arrive at different times and the pulse broadens (1). A very narrow core reduces it by forcing all rays onto nearly the same path (1). [2]

SECTION C · Stretch

C1 $\sin \theta_c = n_{\text{cladding}} / n_{\text{core}}$ (1)
 $= 1.40 / 1.50$ (1)
 $\theta_c = 69.0^\circ$ (1) [3]

C2 $\sin \theta_c = 1/n = 1/1.5$ (1)
 $\theta_c = 41.8^\circ$ (1)
 45° is greater than the critical angle, so the ray undergoes total internal reflection and does not leave the block (1) [3]

C3 It has a central core of high refractive index surrounded by a cladding of slightly lower refractive index (1). The cladding gives a well-defined boundary for total internal reflection (1), protects the core, and reduces signal loss and crossover between fibres (1). [3]

C4 $\sin \theta_c = n_{\text{cladding}} / n_{\text{core}}$ (1). For P: $\theta_c = 65.2^\circ$; for Q: $\theta_c = 72.5^\circ$ (1); for R: $\theta_c = 80.7^\circ$ (1). Only R gives a critical angle of at least 80° , so the manufacturer should choose cladding R (1). [4]

C5 $v = c/n = (3.0 \times 10^8) / 1.48$ (1) $= 2.03 \times 10^8 \text{ m s}^{-1}$, which is about $2 \times 10^8 \text{ m s}^{-1}$ (1). $t = d/v = (15 \times 10^3) / (2.03 \times 10^8)$ (1) $= 7.4 \times 10^{-5} \text{ s}$ (1). [4]

C6 Modal dispersion: rays reflecting at different angles travel different total path lengths along the fibre (1), so parts of the same pulse arrive at different times and the pulse spreads out (1). A very narrow core reduces this by forcing every ray onto nearly the same path (1). Material dispersion: different wavelengths travel at slightly different speeds in the glass, so a pulse of non-monochromatic light spreads in time (1); using monochromatic light (a single wavelength, for example from a laser) removes this spread (1). Broadened pulses can overlap their neighbours so that individual pulses can no longer be distinguished; pulses must therefore be sent less often, limiting the data rate (1). [6]