



QUESTION WORKBOOK

# Wave-particle duality

Quantum phenomena · Year 12

AQA 3.2.2.4 · CIE 22.3.1, 22.3.2, 22.3.3, 22.3.4 · OCR A 4.5.3(a), 4.5.3(b), 4.5.3(c)

19 questions · 55 marks

PRINT EDITION

**SECTION A** · Warm-up

- A1** State the two pieces of evidence showing that light and electrons each have both wave and particle properties. [2]

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- A2** A particle has a momentum of  $2.0 \times 10^{-24} \text{ kg m s}^{-1}$ . Calculate its de Broglie wavelength ( $h = 6.63 \times 10^{-34} \text{ J s}$ ). [2]

- A3** State the de Broglie equation and define each term. [2]

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- A4** The electrons in an electron microscope have a de Broglie wavelength of  $1.2 \times 10^{-10} \text{ m}$ . Calculate their momentum ( $h = 6.63 \times 10^{-34} \text{ J s}$ ). [2]

- A5** State the condition needed for a beam of particles to be diffracted appreciably by the atoms of a crystal. [1]

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- A6** The momentum of a particle is doubled. State what happens to its de Broglie wavelength. [1]

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**SECTION B** · Standard

- B1** An electron moves at  $1.0 \times 10^6 \text{ m s}^{-1}$ . Calculate its de Broglie wavelength ( $m_e = 9.11 \times 10^{-31} \text{ kg}$ ). [3]

- B2** An electron is accelerated from rest through a potential difference of 100 V. Calculate (a) its speed and (b) its de Broglie wavelength ( $e = 1.60 \times 10^{-19} \text{ C}$ ,  $m_e = 9.11 \times 10^{-31} \text{ kg}$ ). [4]

- B3** An electron and a proton travel at the same speed of  $1.0 \times 10^5 \text{ m s}^{-1}$ . Calculate the de Broglie wavelength of each ( $m_p = 1.67 \times 10^{-27} \text{ kg}$ ) and state which is larger. [3]

- B4** Explain what the diffraction of electrons by a thin crystal shows about the nature of electrons. [3]

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- B5** In an experiment to show that whole atoms have wave properties, a beam of helium atoms is directed at a crystal whose atomic spacing is  $1.0 \times 10^{-10}$  m. Calculate the speed at which a helium atom, of mass  $6.6 \times 10^{-27}$  kg, has a de Broglie wavelength equal to this spacing ( $h = 6.63 \times 10^{-34}$  J s). [3]

- B6** An electron travels at  $3.3 \times 10^6$  m s<sup>-1</sup>. Determine the speed at which a proton would have the same de Broglie wavelength as this electron ( $m_e = 9.11 \times 10^{-31}$  kg,  $m_p = 1.67 \times 10^{-27}$  kg). [3]

- B7** In a molecular-beam experiment, molecules travelling at  $500 \text{ m s}^{-1}$  produce a diffraction pattern corresponding to a de Broglie wavelength of  $2.8 \times 10^{-11} \text{ m}$ . The beam is one of: helium (particle mass  $6.6 \times 10^{-27} \text{ kg}$ ), nitrogen ( $4.7 \times 10^{-26} \text{ kg}$ ) or oxygen ( $5.3 \times 10^{-26} \text{ kg}$ ). Determine the mass of one molecule and deduce which gas the beam contains ( $h = 6.63 \times 10^{-34} \text{ J s}$ ). [4]

### SECTION C · Stretch

- C1** A cricket ball of mass  $0.16 \text{ kg}$  is bowled at  $30 \text{ m s}^{-1}$ . Calculate its de Broglie wavelength and explain why no diffraction of the ball is ever observed. [4]

- C2** Calculate the accelerating potential difference needed to give an electron a de Broglie wavelength of  $1.0 \times 10^{-10} \text{ m}$  ( $h = 6.63 \times 10^{-34} \text{ J s}$ ,  $m_e = 9.11 \times 10^{-31} \text{ kg}$ ,  $e = 1.60 \times 10^{-19} \text{ C}$ ). [4]

- C3** Explain how and why the electron diffraction pattern changes when the electrons are accelerated to a higher speed. [3]

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- C4** A researcher wants to study a crystal whose atomic plane spacing is  $2.0 \times 10^{-10} \text{ m}$  by diffraction. Two beams are available: electrons moving at  $1.0 \times 10^7 \text{ m s}^{-1}$ , or neutrons moving at  $2.0 \times 10^3 \text{ m s}^{-1}$ . Deduce which beam is better matched to the crystal ( $h = 6.63 \times 10^{-34} \text{ J s}$ ,  $m_e = 9.11 \times 10^{-31} \text{ kg}$ , neutron mass =  $1.67 \times 10^{-27} \text{ kg}$ ). [4]

- C5** Show that the kinetic energy of a particle of mass  $m$  with de Broglie wavelength  $\lambda$  is given by  $E_k = h^2/(2m\lambda^2)$ . Go on to calculate the kinetic energy of an electron whose de Broglie wavelength is  $5.0 \times 10^{-10} \text{ m}$  ( $h = 6.63 \times 10^{-34} \text{ J s}$ ,  $m_e = 9.11 \times 10^{-31} \text{ kg}$ ). [4]

- C6** The smallest detail a microscope can resolve is roughly the size of the wavelength it uses. Visible light has wavelengths around  $5 \times 10^{-7} \text{ m}$ ; the electrons in an electron microscope have a de Broglie wavelength of about  $1 \times 10^{-11} \text{ m}$ . Explain why an electron microscope can resolve far finer detail than an optical microscope.

[3]

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